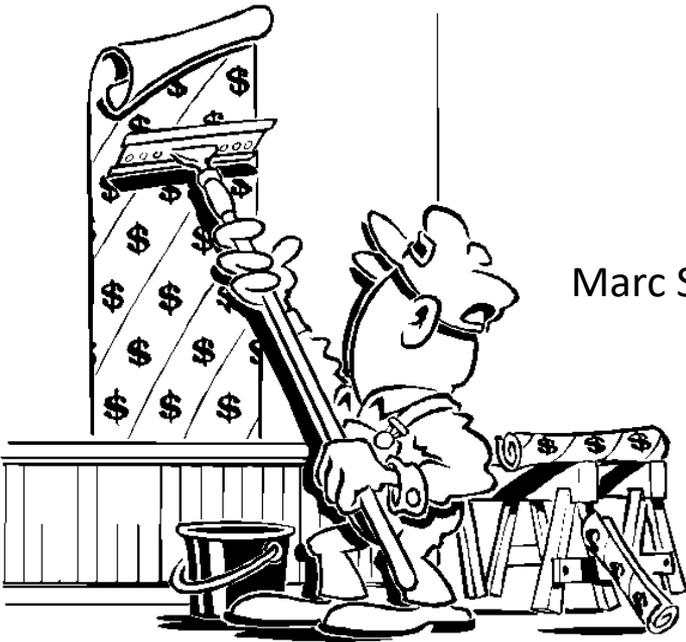


Lecture #10

Texture Mapping

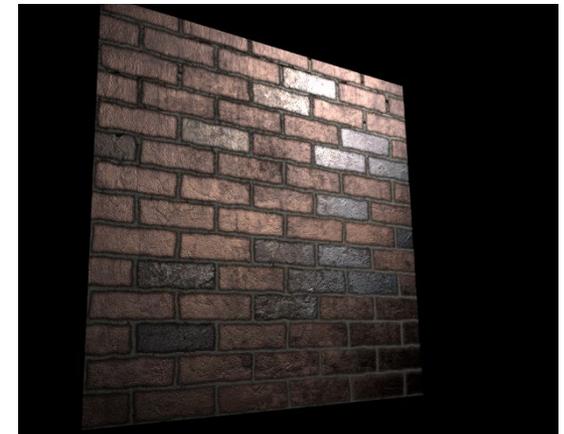
Computer Graphics
Winter Term 2020/21

Marc Stamminger / Roberto Grosso



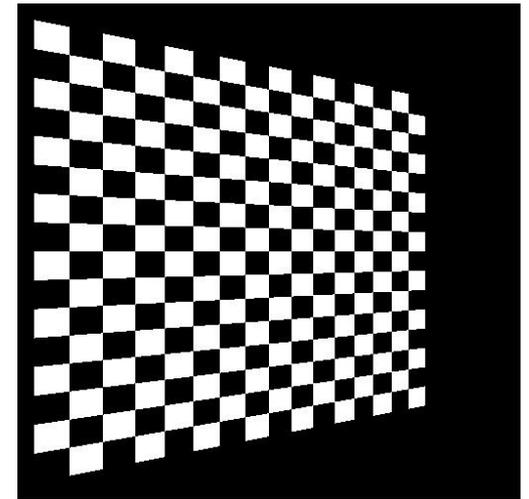
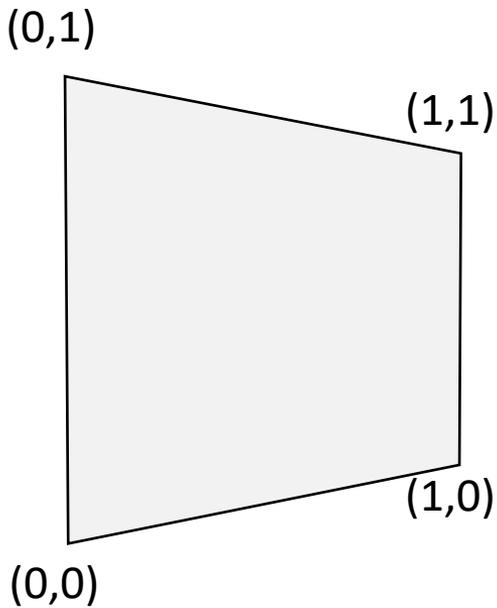
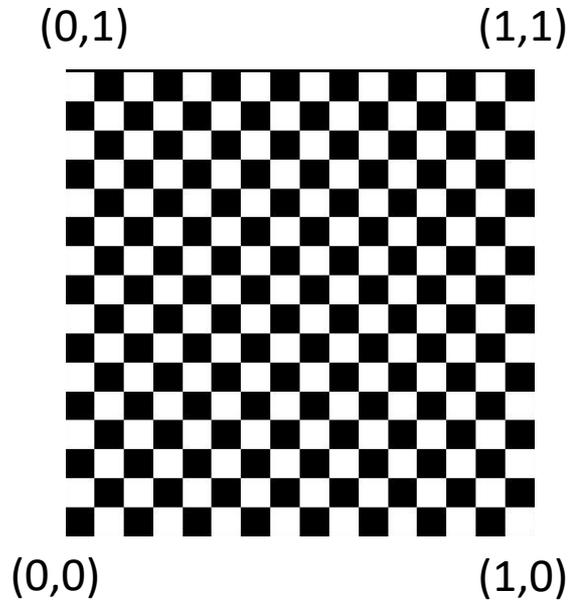
Texture Mapping

- so far: detail through polygons & materials
- example: (large) brick wall
 - many polygons & materials needed for bricks
→ inefficient for memory and processing
- alternative: **Textures**
introduced by Ed Catmull (1974)
extended by Jim Blinn (1976)



Texture Mapping

- Texture + Quad = Image



Texture Mapping



Foley, van Dam, Feiner, Hughes

Texture Mapping



Foley, van Dam, Feiner, Hughes

Texture Mapping

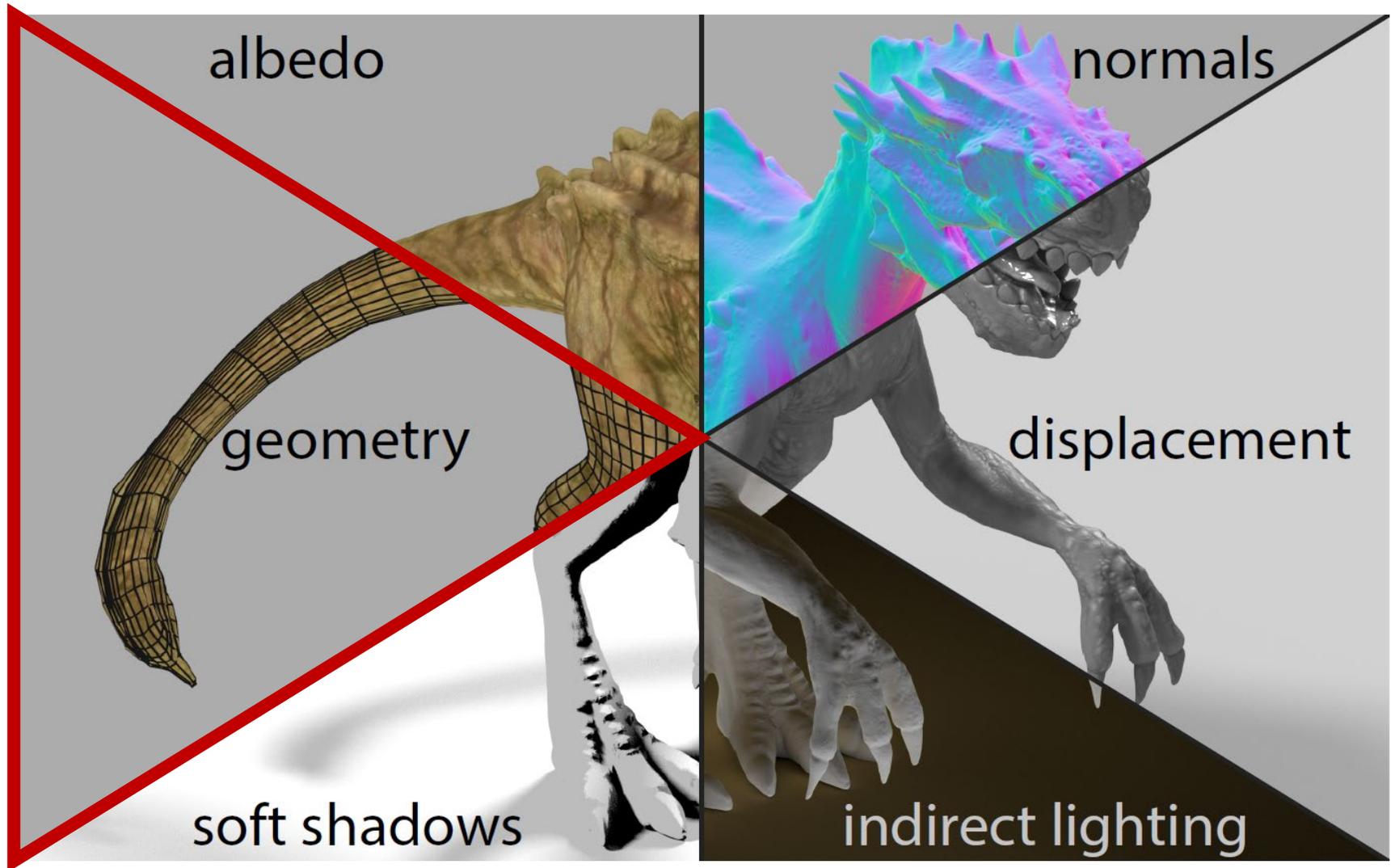
- What are textures or texture maps?
 - Functions or images that change the appearance of an object, typically its color
 - Coarse geometry (i.e. fast rendering), fine texture (i.e. fine visual detail)
 - Great performance gain compared to using huge triangle meshes with different materials
 - Can be 1D
 - heat map: maps the “temperature” of an object to color(cold=blue, warm=red)
 - or 2D
 - images to mapped onto the object like wall paper
 - or 3D
 - volumetric objects such as clouds
 - or solid objects such as wood
- **for now, we only look at 2D textures**

Texture Mapping

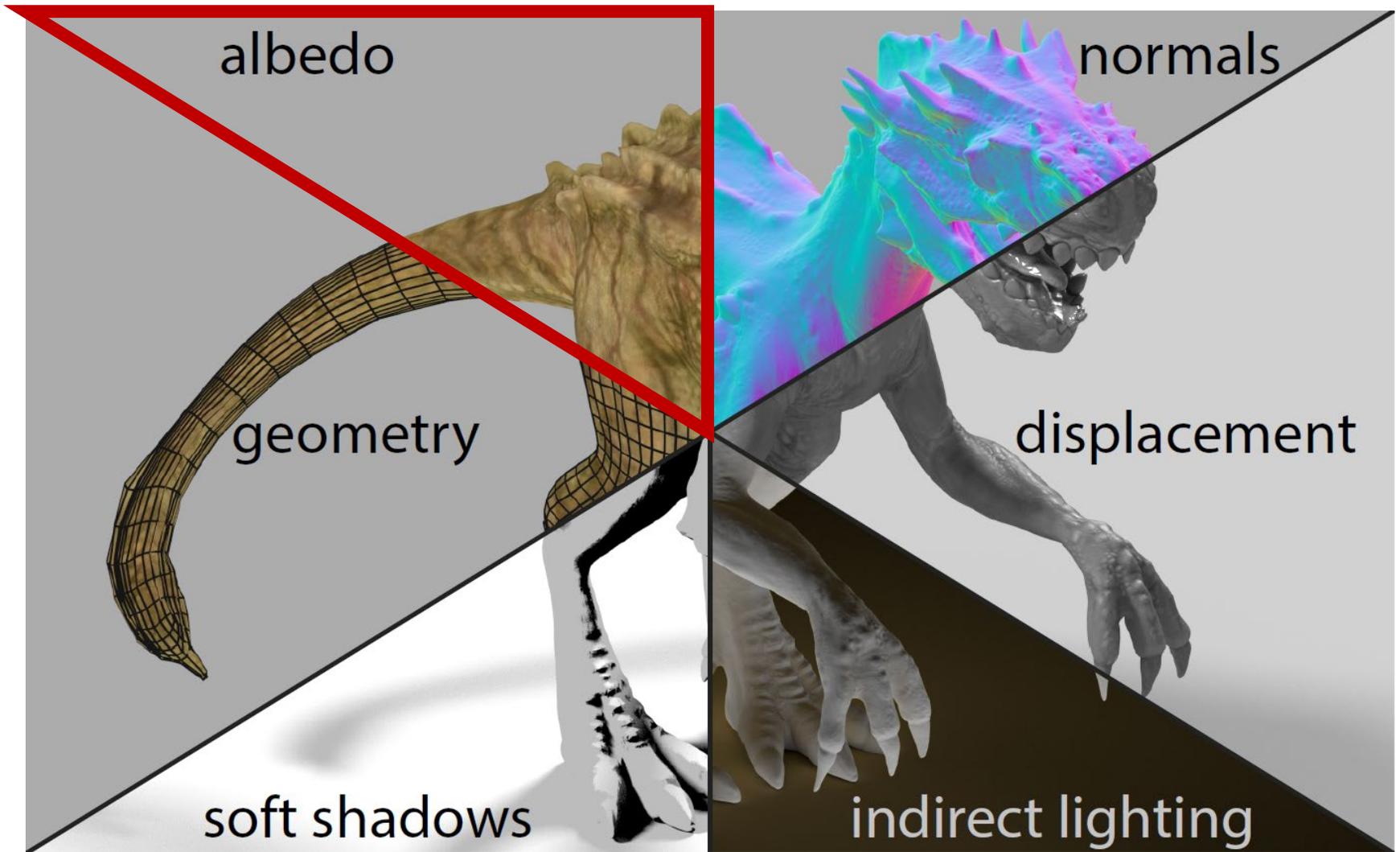
- Textures usually contain color, e.g. the diffuse component of the Phong model
- But they can also contain specular color, ambient color or other material parameters
- And even much more!



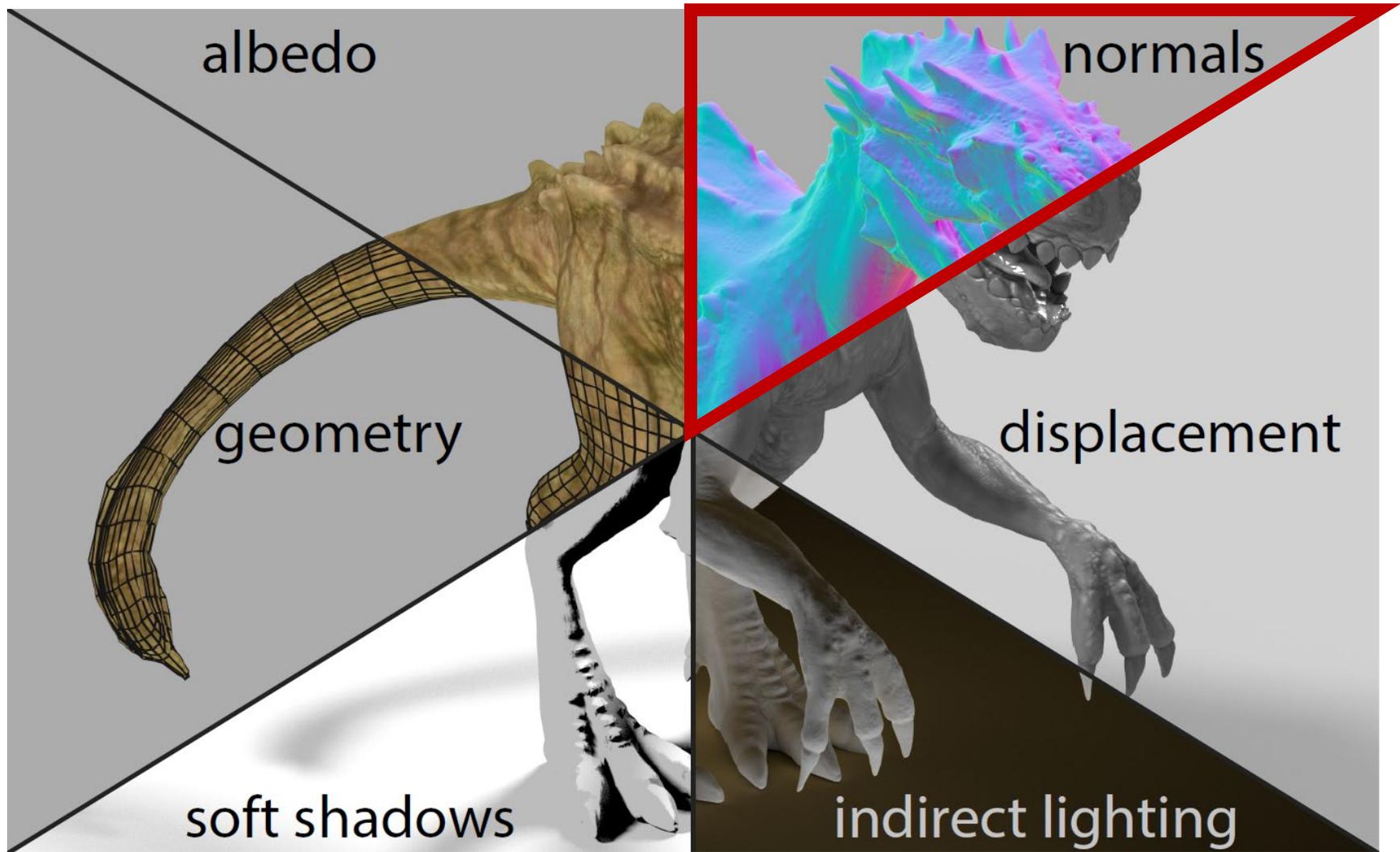
Texture Mapping - Introduction



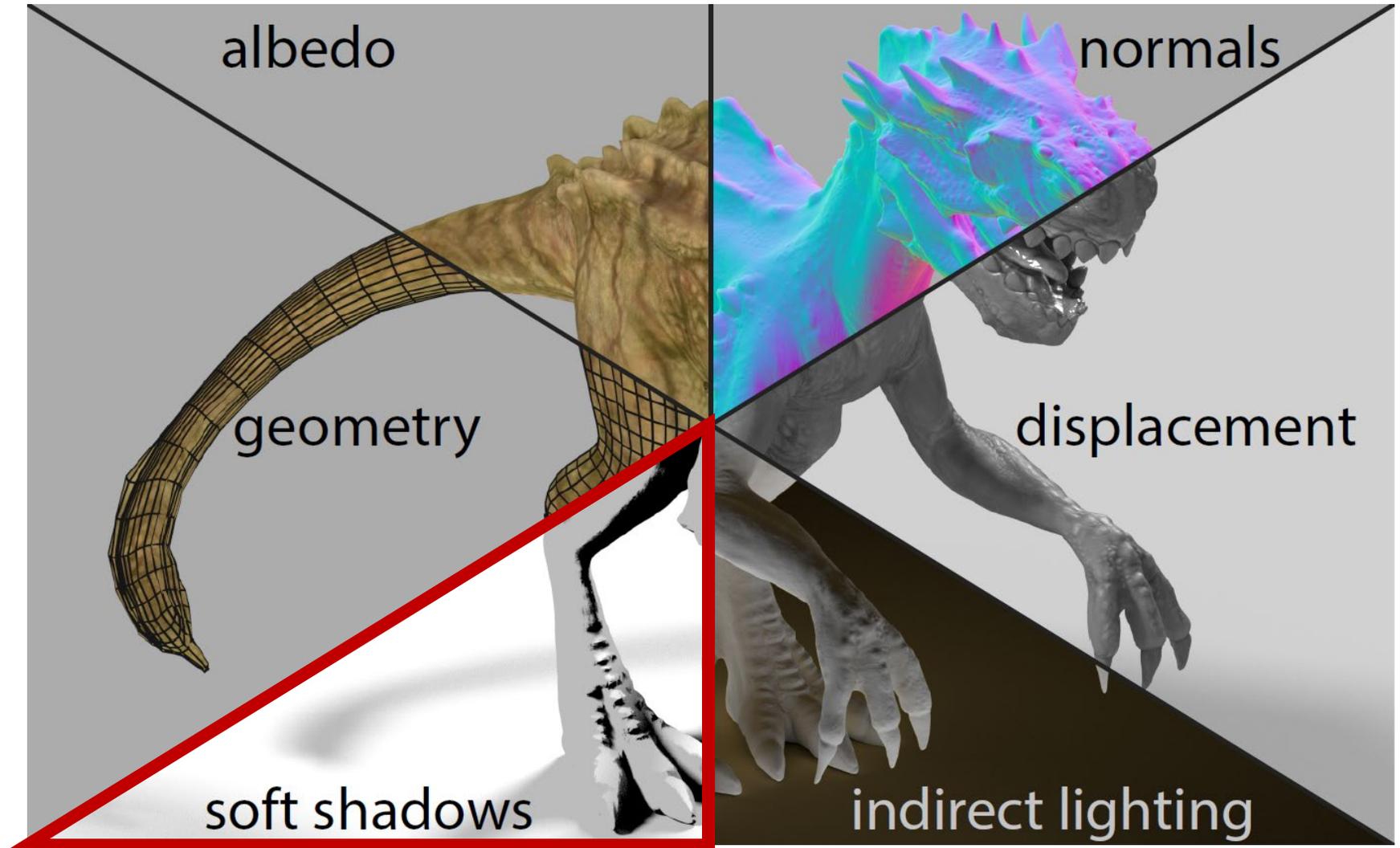
Texture Mapping - Introduction



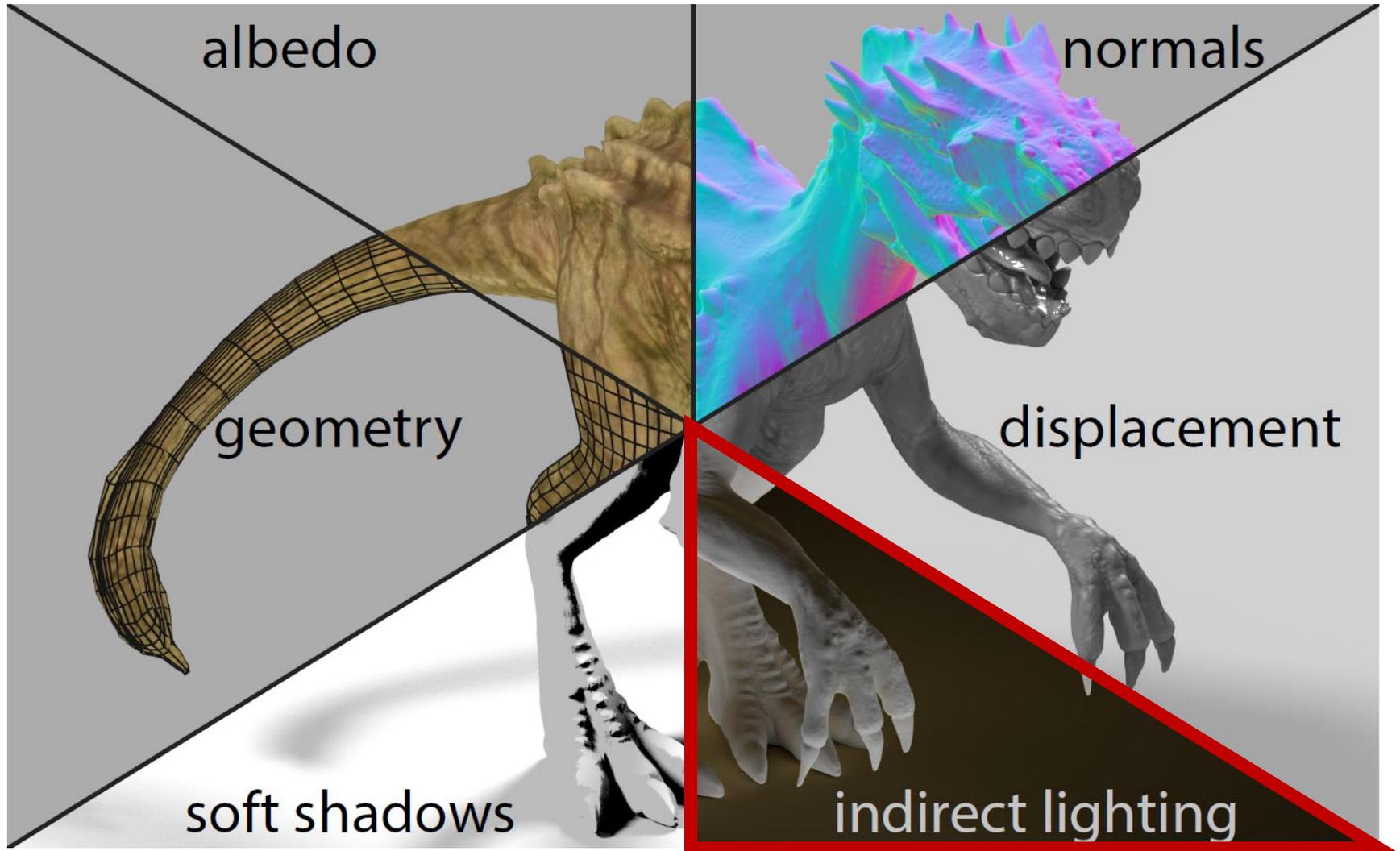
Texture Mapping - Introduction



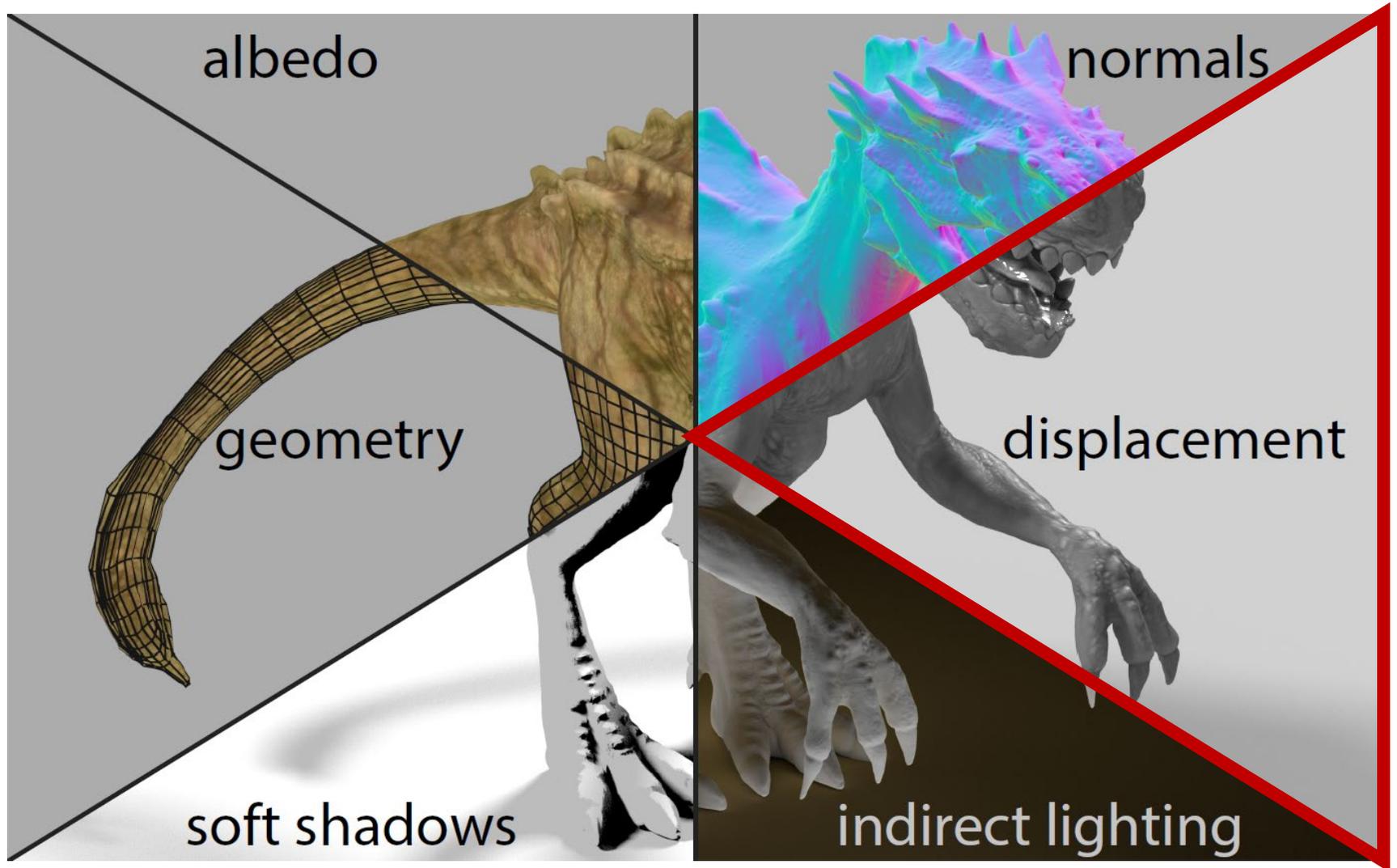
Texture Mapping - Introduction



Texture Mapping - Introduction



Texture Mapping - Introduction



Texture Mapping

- Mapping in 2D:

- Texture image of size (n_x, n_y)
- Constraints on some architectures (powers of 2)
- Texture coordinates “s” and “t” for accessing texture images
 - (s, t, r) in 3D and
 - (s, t, r, q) homogeneous texture coordinates
- Assign to every geometric point (x, y, z) on the polygon \mathbf{P} a texture coordinate (s, t) :

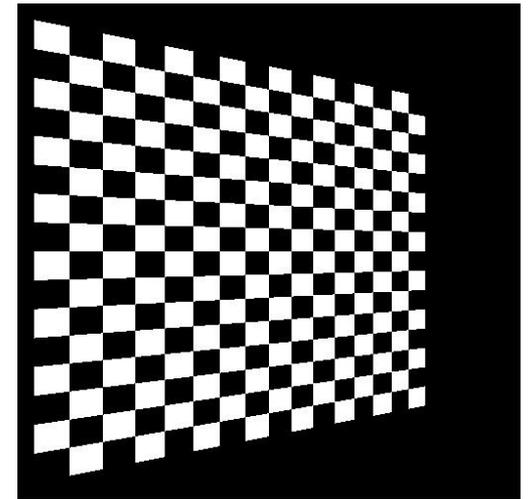
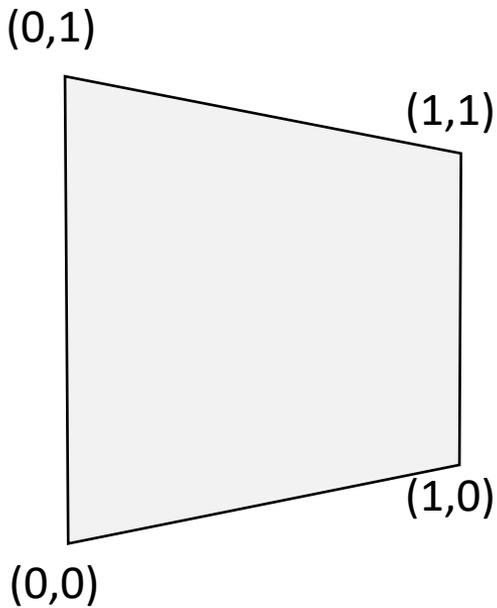
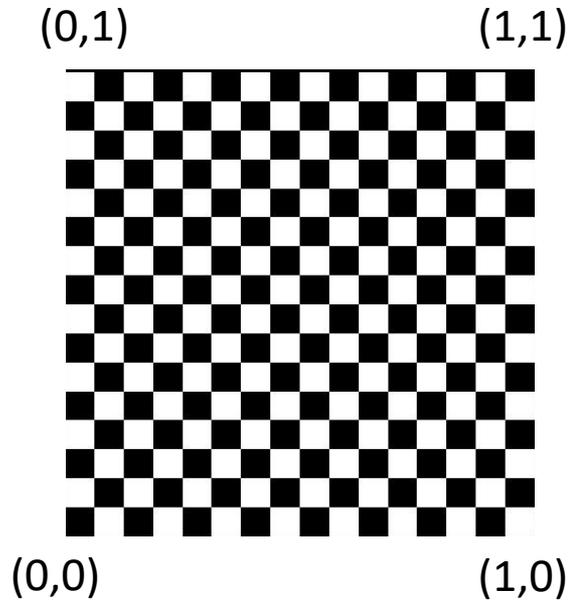
$$\rightarrow F: P \in \mathbb{R}^3 \rightarrow [0,1]^2 \in \mathbb{R}^2$$

- Simple procedure:

1. for every vertex assign (s, t) .
2. For interior points assign (s, t) by interpolation.

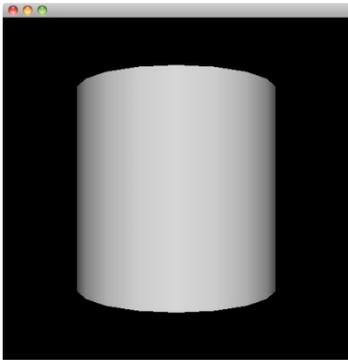
Texture Mapping

• Texture + Quad = Image

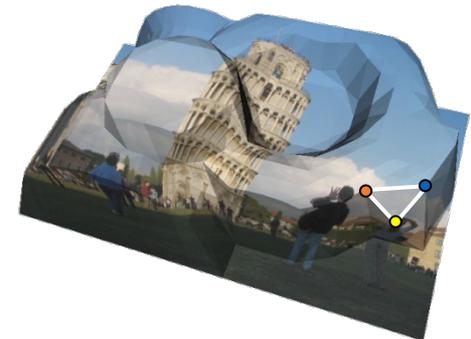
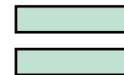
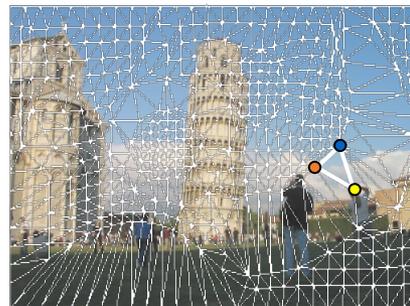
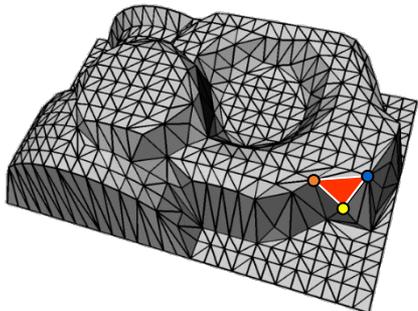


Parameterization

- Texture coordinates \rightarrow **Parameterization**
- Simple parameterization

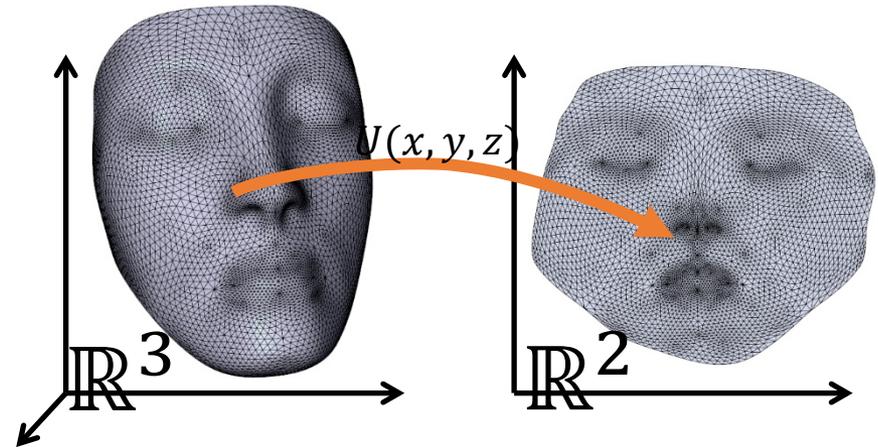


- difficult parameterization



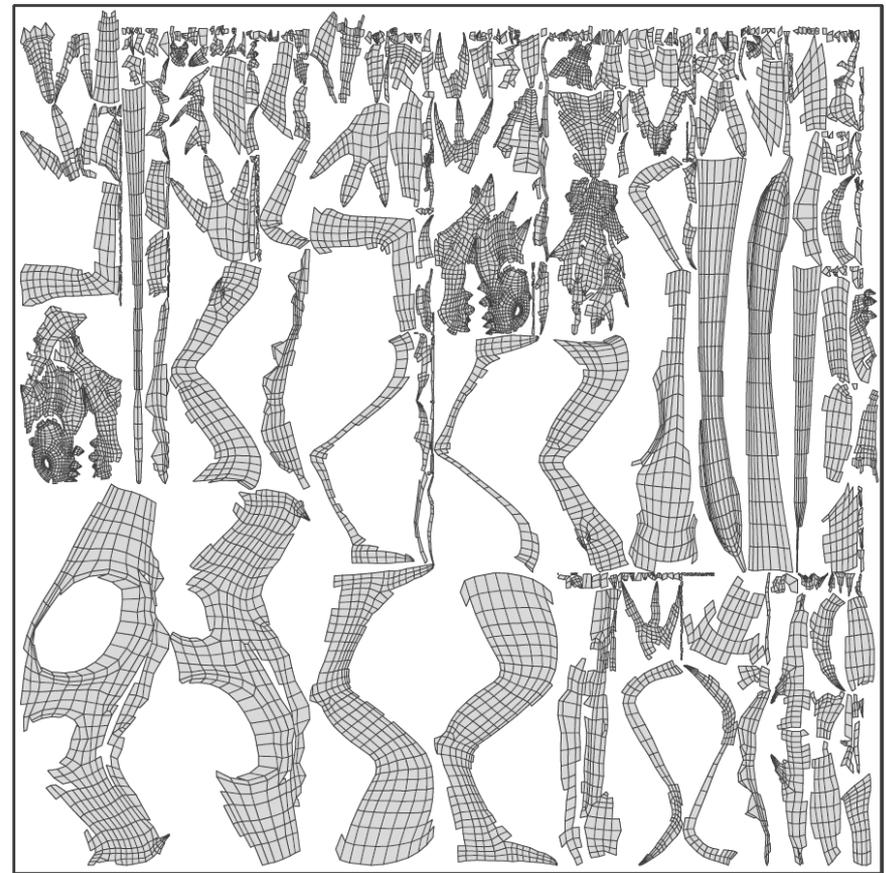
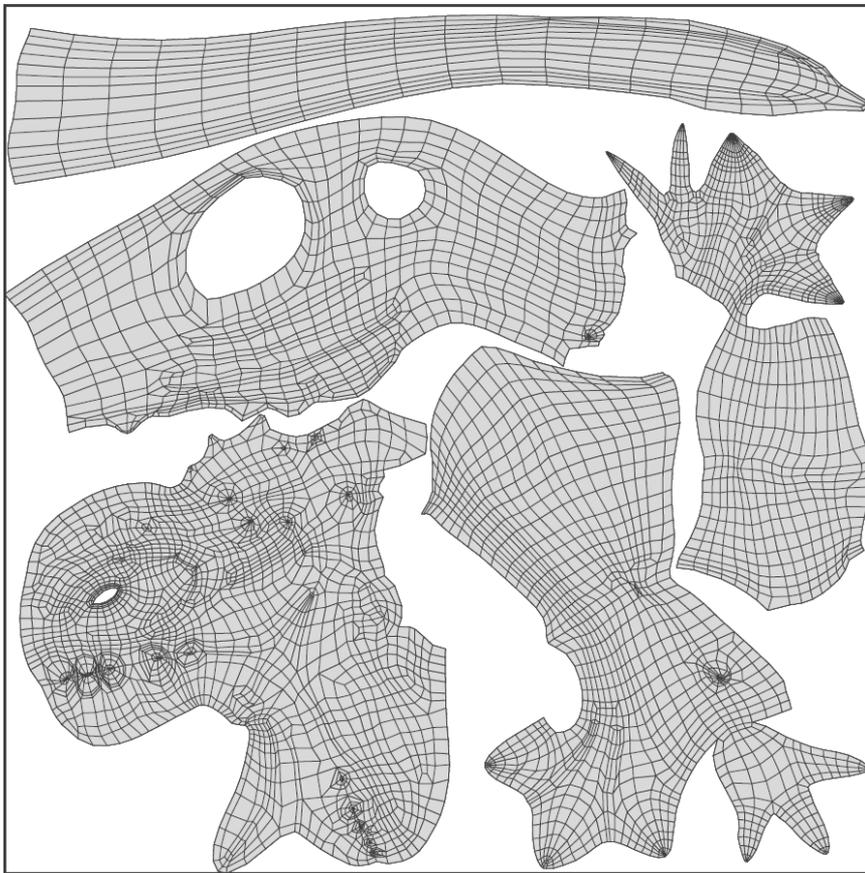
Parameterization

- Find a mapping from 3D surface to 2D plane (or vice versa)
- Long standing problem
- solutions available in modeling programs, often not robust
- → lecture „**Geometry Processing**“



Parameterization

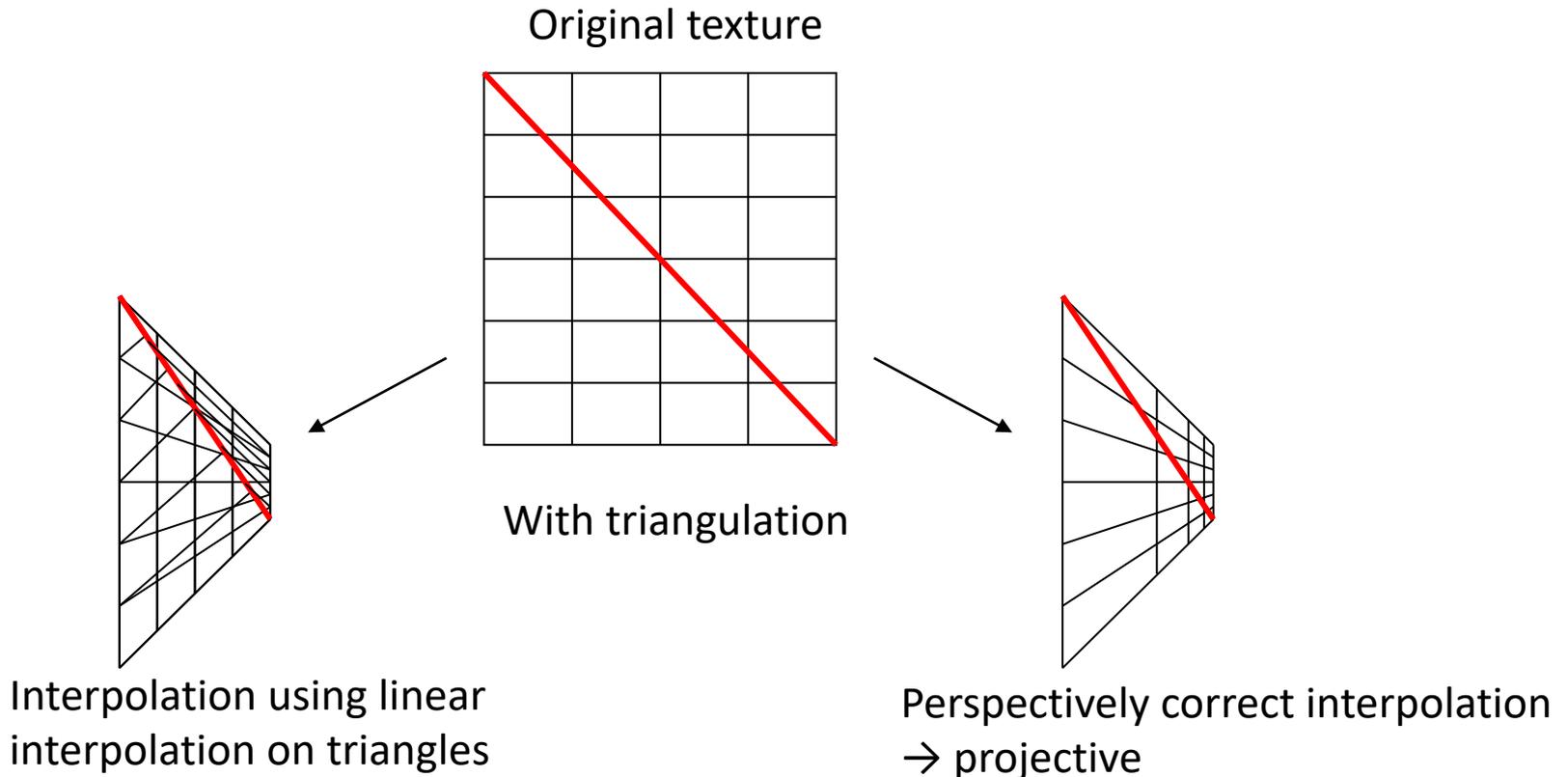
- **Texture Atlas:**
not one single texture, but fragmented textures for object parts



Texture Mapping for Rasterized Triangles

- Interpolation Problem

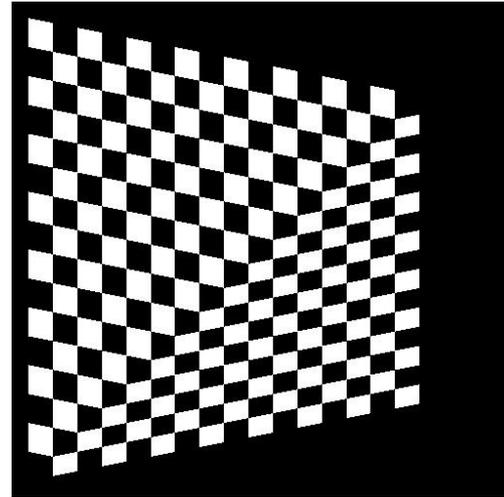
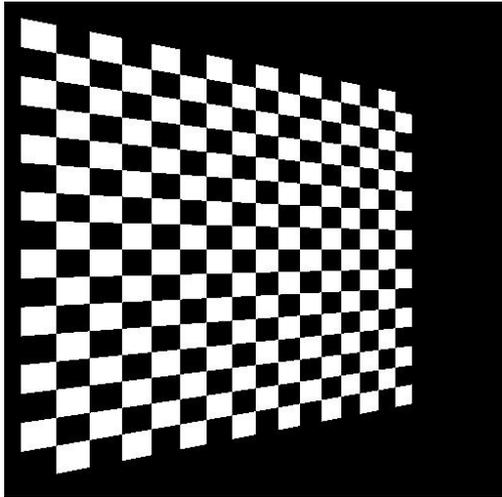
- Standard interpolation method at rasterization stage (linear interpolation) results in distorted images!
- Reason: Does not consider the distortion of the perspective transformation!



Texture Mapping for Rasterized Triangles

- Correct

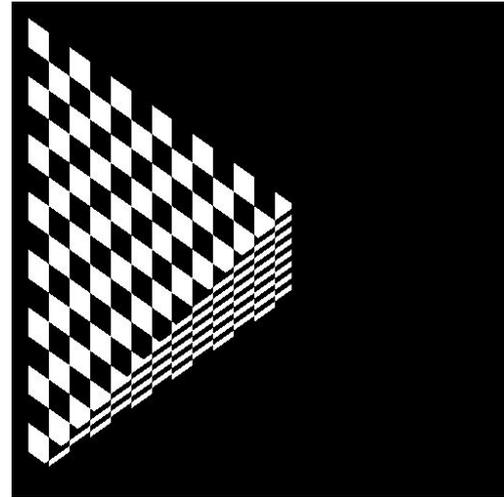
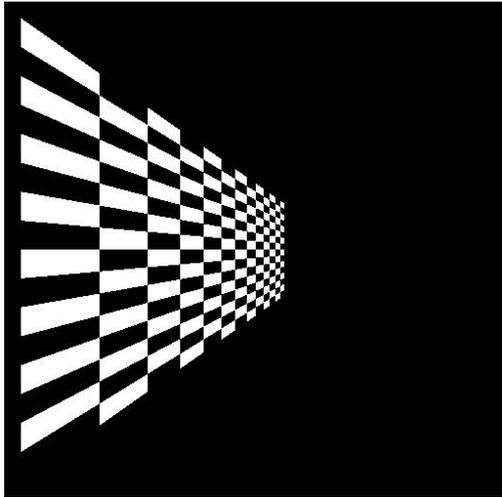
wrong



Texture Mapping for Rasterized Triangles

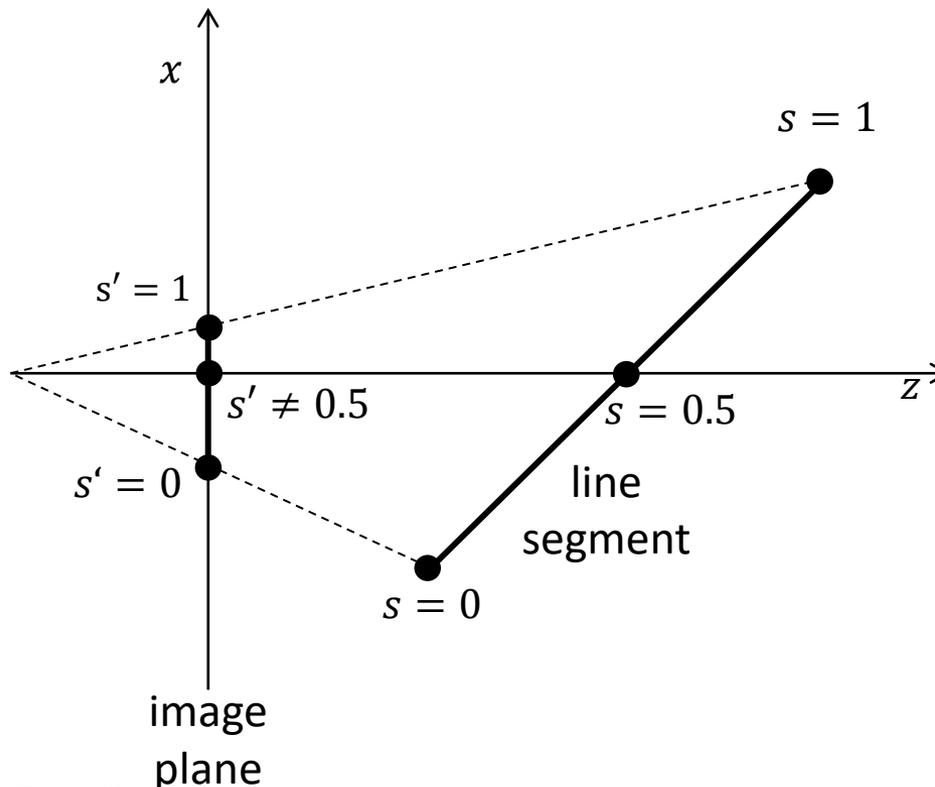
- Correct

very wrong



Texture Mapping for Rasterized Triangles

- Perspective interpolation – problem statement
 - Example: line segment not parallel to image plane:
 - s : texture coordinate in world space, s' : texture coordinate in screen space
 - Linear interpolation of s' in screen space does not match interpolation of s in world coordinates.



Texture Mapping for Rasterized Triangles

- Perspective Interpolation
 - Needed: Mapping $s' \rightarrow s$ that implements perspective correct linear interpolation in screen space
 - Solution: consider the division by z !
 - following derivation from http://www.comp.nus.edu.sg/~lowkl/publications/lowk_persp_interp_techrep.pdf

Texture Mapping for Rasterized Triangles

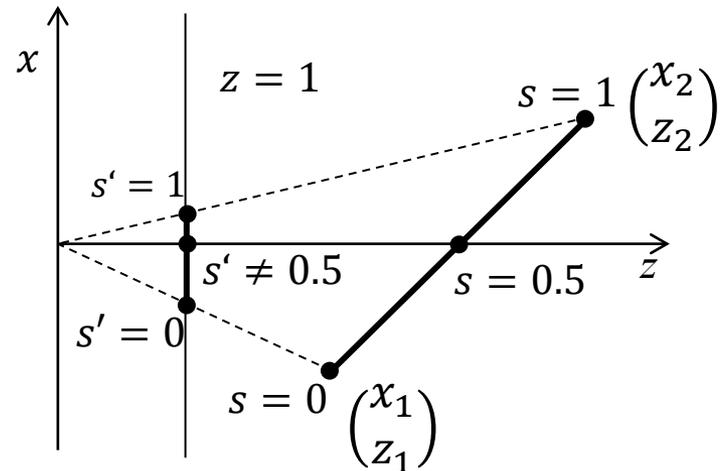
- s : relative position in world space, s' in image space
- In world space, we describe the line segment as:

$$\begin{pmatrix} x \\ z \end{pmatrix} = \begin{pmatrix} x_1 \\ z_1 \end{pmatrix} + s \begin{pmatrix} x_2 - x_1 \\ z_2 - z_1 \end{pmatrix}$$

- in image space:

$$x' = \frac{x_1}{z_1} + s' \left(\frac{x_2}{z_2} - \frac{x_1}{z_1} \right)$$

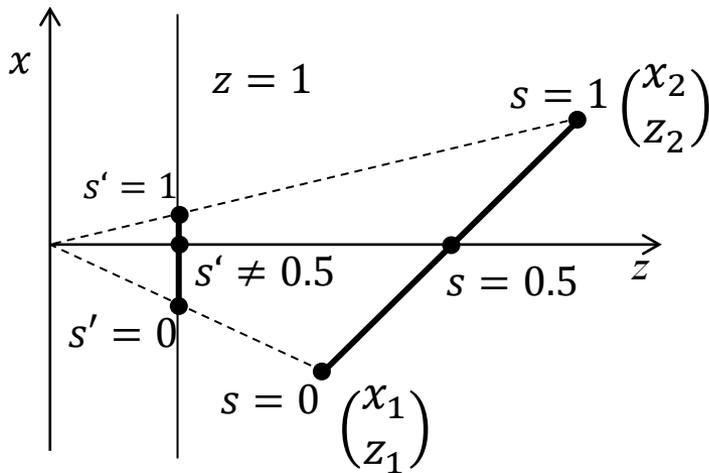
- Obviously s' is not the same as s !



Texture Mapping for Rasterized Triangles

- During rasterization, we know s' , and need to derive s from s'
- with some arithmetics, we find

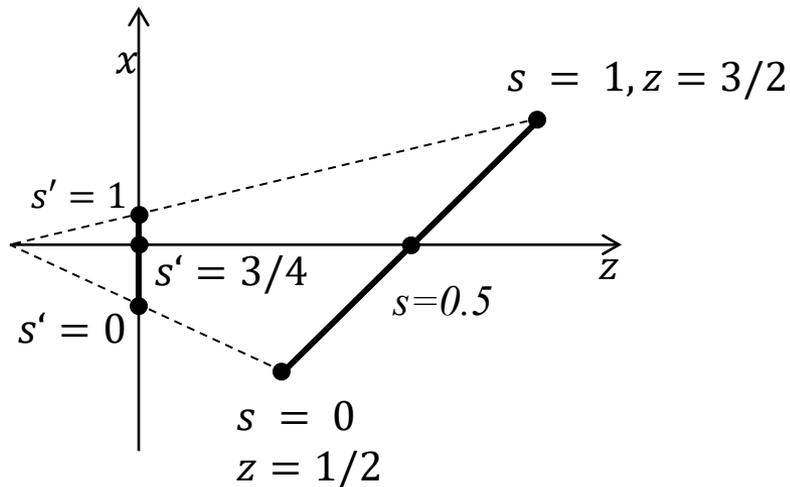
$$s = \frac{s'z_1}{s'z_1 + (1 - s')z_2}$$



Texture Mapping for Rasterized Triangles

- Example

- $s' = \frac{3}{4} \rightarrow s = \frac{\frac{3}{4}z_1}{\frac{3}{4}z_1 + \frac{1}{4}z_2} = \frac{1}{2}$

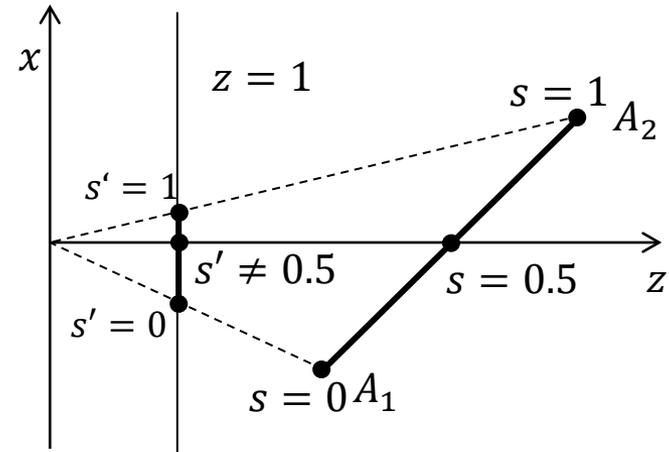


Texture Mapping for Rasterized Triangles

- for arbitrary attributes A along a line:
 - z -values z_1 and z_2
 - attribute values A_1 and A_2

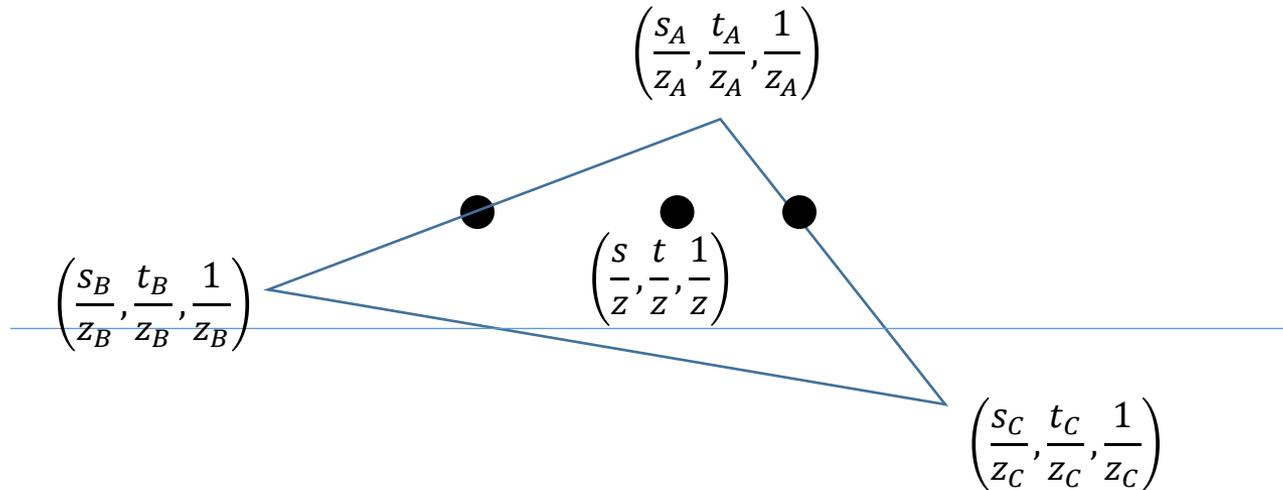
- $$A(s) = A_1 + s(A_2 - A_1) = \dots = \frac{\frac{A_1}{z_1} + s' \left(\frac{A_2}{z_2} - \frac{A_1}{z_1} \right)}{\frac{1}{z_1} + s' \left(\frac{1}{z_2} - \frac{1}{z_1} \right)}$$

- Interpolate A/z and $1/z$
- divide to get interpolated A



Texture Mapping for Rasterized Triangles

- From this, we can derive an approach for interpolating texture coordinates
 - interpolate s/z , t/z , and $1/z$ during rasterization
 - Per pixel: $(s/z)/(1/z), (t/z)/(1/z) \rightarrow (s, t)$



- Also works for arbitrary attributes

Texture Mapping

- In OpenGL / WebGL:
 - 1D, 2D and 3D textures
 - textures can have luminance only (grey value), luminance plus alpha, color, or color plus alpha
 - 8bit per channel, 16bit per channel, or float values
 - are sampled in a shader using a **sampler** object
 - homogeneous texture coordinates (s, t, r, q)
 - newer OpenGL also supports compressed textures

Texture Mapping

- In WebGL

```
if (!texHandle) {
    var image = document.getElementById(„mytexture“);
    texHandle = gl.createTexture();
    gl.bindTexture(gl.TEXTURE_2D, texHandle);
    gl.texImage2D(gl.TEXTURE_2D, 0, gl.RGBA, gl.RGBA,
        gl.UNSIGNED_BYTE, image);
} else
    gl.bindTexture(gl.TEXTURE_2D, texHandle);
```

- pixel shader

```
...
uniform sampler2D texture;
varying vec2 uv; // texture coordinate

void main(void) {
    ...
    // finally, apply texture by multiplication
    gl_FragColor *= texture2D(texture, uv);
}
```

Texture Mapping Demo

Textures



Texture Magnification

NEAREST

LINEAR

Texture Minification

NEAREST - No MIPMap

LINEAR - No MIPMap

NEAREST_MIPMAP_NEAREST

LINEAR_MIPMAP_NEAREST

NEAREST_MIPMAP_LINEAR

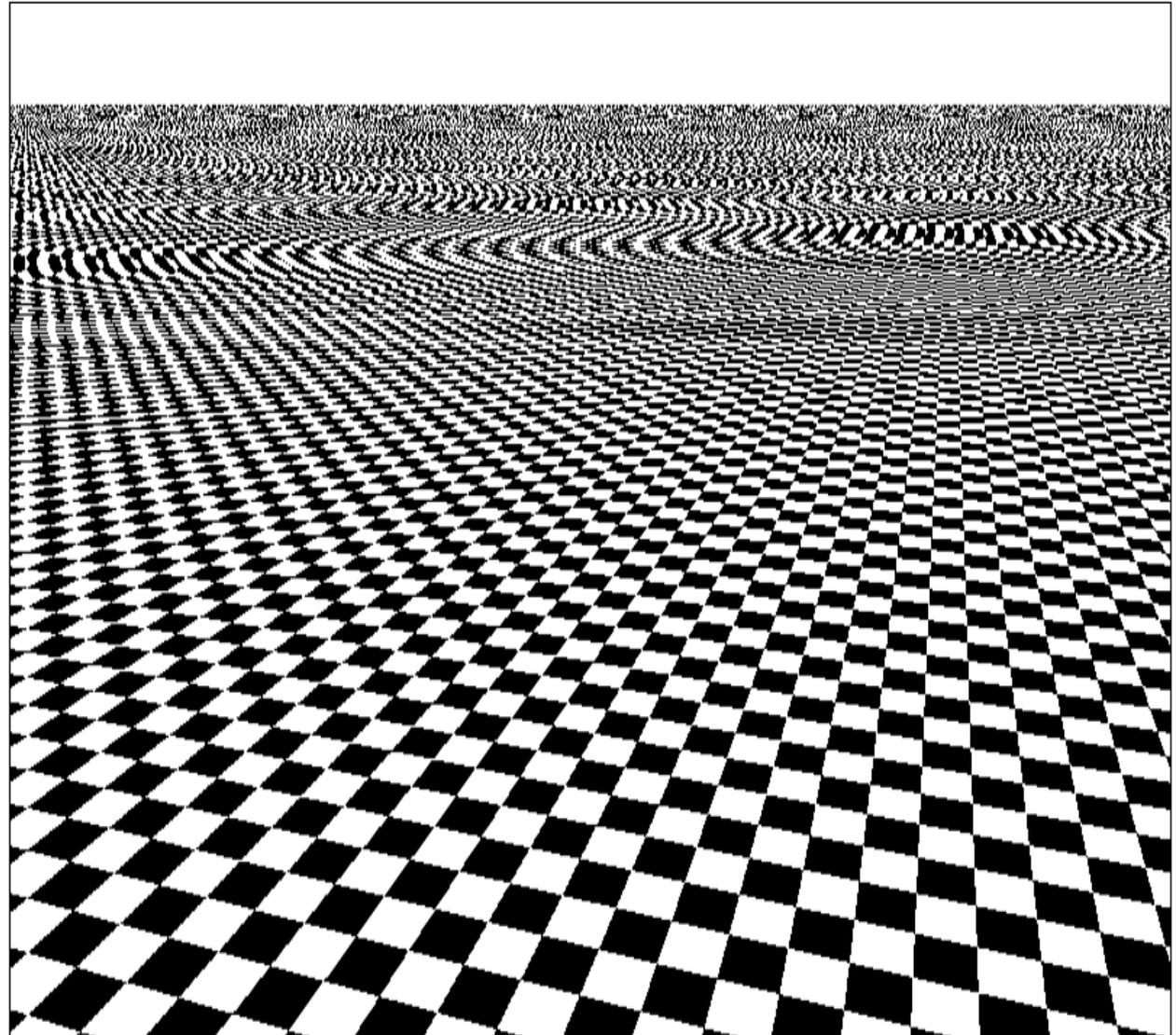
LINEAR_MIPMAP_LINEAR

Patch

Infinite Patch

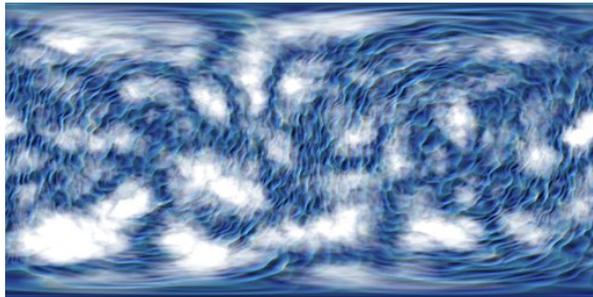
Mirror Patch

Normal Map

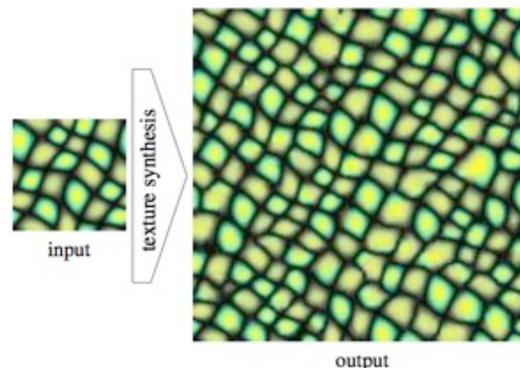


Procedural Texture Generation

- Textures can come from an image file, e.g. jpg
- or can be generated by a procedure
 - on the fly in a shader
 - often based on fractal noise or turbulence functions (see later)



- → Texture synthesis: generate arbitrarily large high-quality texture from a small input sample.



Procedural Texture Generation

- regular stripes dark/bright brown
- Stripe width/distance: varies over years
- Shape of stripes slightly unregular
- Less or more irregular patterns possible
- Example:
<https://www.shadertoy.com/view/ldscDM>



freestocktextures.com

Procedural Texture Generation

- Procedural texture generation
 - Computer generated texture image (1D, 2D or 3D) created using an algorithm.
 - Natural appearance requires some randomness, but also structure
 - All based on **Noise Functions**



```
/* Copyrighted Pixar 1988 */
/* From the RenderMan Companion p. 255 */
/* Listing 16.19 Blue marble surface shader*/

/*
 * blue_marble(): a marble stone texture in shades of blue
 * surface
 */

blue_marble(
    float
        Ks = .4,
        Kd = .6,
        Ka = .1,
        roughness = .1,
        txtscale = 1,
        color specularcolor = 1)
{
    point PP; /* scaled point in shader space */
    float csp; /* color spline parameter */
    point Nf; /* forward-facing normal */
    point V; /* for specular() */
    float pixelsize, twice, scale, weight, turbulence;

    /* Obtain a forward-facing normal for lighting calculations. */
    Nf = faceforward( normalize(N), I);
    V = normalize(-I);

    /*
     * Compute "turbulence" a la [PERLINS]. Turbulence is a sum of
     * "noise" components with a "fractal" 1/f power spectrum. It gives the
     * visual impression of turbulent fluid flow (for example, as in the
     * formation of blue_marble from molten color splines). Use the
     * surface element area in texture space to control the number of
     * noise components so that the frequency content is appropriate
     * to the scale. This prevents aliasing of the texture.
     */
    PP = transform("shader", P) * txtscale;
    pixelsize = sqrt(area(PP));
    twice = 2 * pixelsize;
    turbulence = 0;
    for (scale = 1; scale > twice; scale /= 2)
        turbulence += scale * noise(PP/scale);

    /* Gradual fade out of highest-frequency component near limit */
    if (scale > pixelsize) {
        weight = (scale / pixelsize) - 1;
        weight = clamp(weight, 0, 1);
        turbulence += weight * scale * noise(PP/scale);
    }

    /*
     * Magnify the upper part of the turbulence range 0.75:1
     * to fill the range 0:1 and use it as the parameter of
     * a color spline through various shades of blue.
     */
    csp = clamp(4 * turbulence - 3, 0, 1);
    Ci = color spline(csp,
        color (0.25, 0.25, 0.35), /* pale blue */
        color (0.25, 0.25, 0.35), /* pale blue */
        color (0.20, 0.20, 0.30), /* medium blue */
        color (0.20, 0.20, 0.30), /* medium blue */
        color (0.20, 0.20, 0.30), /* medium blue */
        color (0.25, 0.25, 0.35), /* pale blue */
        color (0.15, 0.15, 0.25), /* pale blue */
        color (0.15, 0.15, 0.25), /* medium dark blue */
        color (0.15, 0.15, 0.25), /* medium dark blue */
        color (0.10, 0.10, 0.20), /* dark blue */
        color (0.10, 0.10, 0.20), /* dark blue */
        color (0.25, 0.25, 0.35), /* pale blue */
        color (0.10, 0.10, 0.20) /* dark blue */
    );

    /* Multiply this color by the diffusely reflected light. */
    Ci *= Ka*ambient() + Kd*diffuse(Nf);

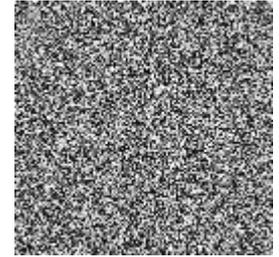
    /* Adjust for opacity. */
    Oi = Os;
    Ci = Ci * Oi;

    /* Add in specular highlights. */
    Ci += specularcolor * Ks * specular(Nf,V,roughness);
}
}
```

Procedural Texture Generation

- **Noise Functions:**

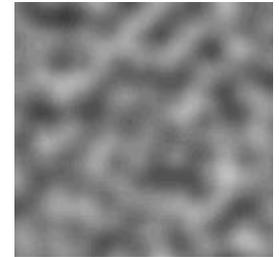
- “White noise”: Assign random color for every point
 - no coherence
 - not helpful for procedural textures
 - **coherency** required



Non coherent

- **Coherent Noise**

- Method for generating coherent noise over space.
- Coherent means: the function values change smoothly.



Coherent

- **First Approach**

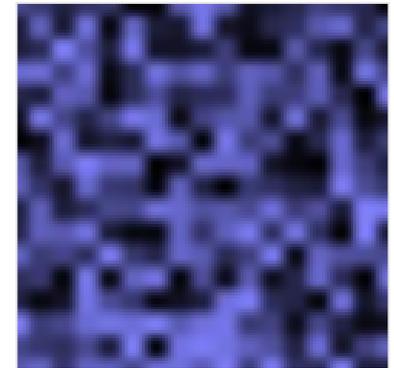
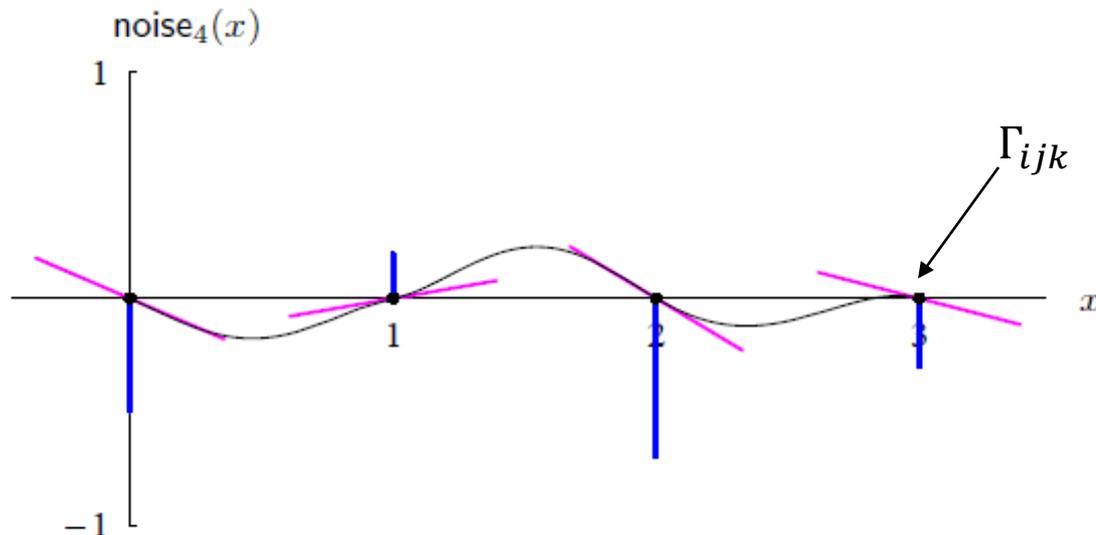
- choose random values on a grid
- interpolate
- grid size corresponds to **noise frequency**

Images by Matt Zucker

Procedural Texture Generation

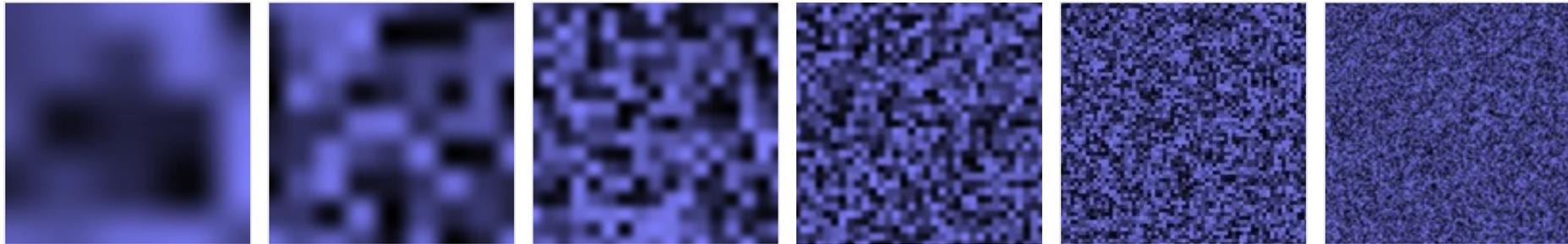
- Better approach, proved very practical: **Perlin Noise**
 - At grid points (i, j, k) choose random **gradient** Γ_{ijk} , set values to zero
 - Γ_{ijk} is determined from (i, j, k) using an array of precomputed random gradient values $G[]$ and a **hash function** $\phi()$ as:
$$\Gamma_{ijk} = G\left(\phi\left(i + \phi\left(j + \phi(k)\right)\right)\right)$$

→ „pseudorandom“ gradient values, very fast to compute
 - Then, these grid point gradients are interpolated

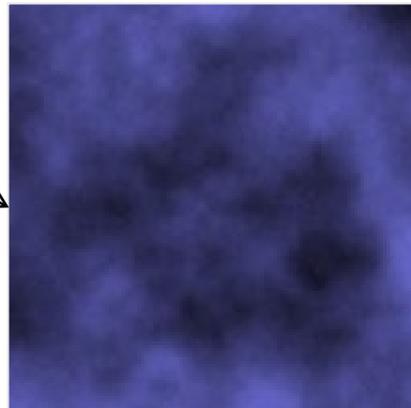


Procedural Texture Generation

- Simple Perlin Noise is boring
- Gets interesting by adding noise of varying frequency:



Sum of all layers

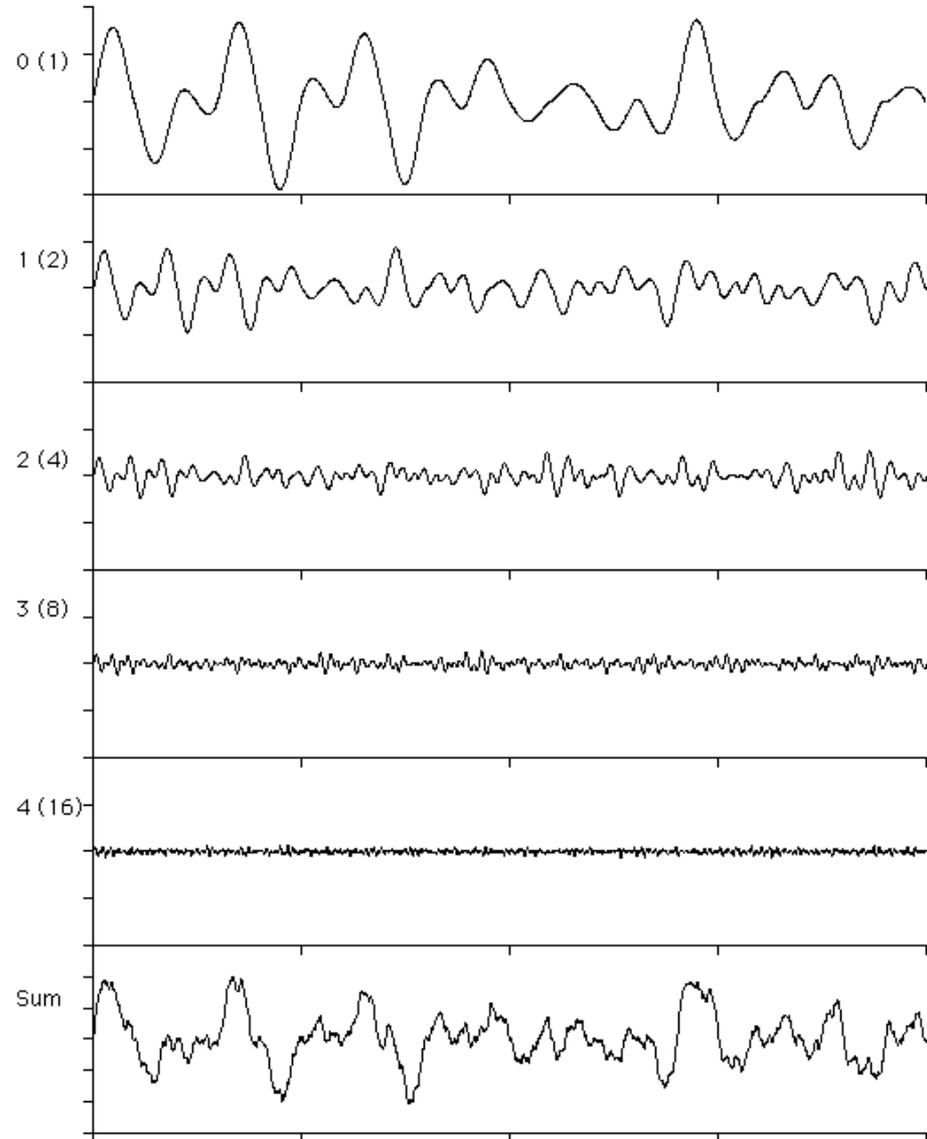


Procedural Texture Generation

- Turbulence

- Many natural textures contain repeating features of different sizes
- Perlin pseudo fractal “turbulence” function
- Effectively adds scaled copies of noise function on top of itself

$$n_t(x) = \sum_i \frac{|n(2^i x)|}{2^i}$$



Procedural Texture Generation

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/* From the RenderMan Companion p. 255 */
/* Listing 16.19 Blue marble surface shader*/

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 * blue_marble(): a marble stone texture in shades of blue
 * surface
 */
blue_marble(
```

```
PP = transform("shader", P) * txtscale;
pixelsize = sqrt(area(PP));
twice = 2 * pixelsize;
turbulence = 0;
for (scale = 1; scale > twice; scale /= 2)
    turbulence += scale * noise(PP/scale);
```

```
/* Gradual fade out of highest-frequency component near limit */
if (scale > pixelsize) {
    weight = (scale / pixelsize) - 1;
    weight = clamp(weight, 0, 1);
    turbulence += weight * scale * noise(PP/scale);
}
```

```
color (0.15, 0.15, 0.26) /* medium dark blue */
color (0.15, 0.15, 0.26) /* medium dark blue */
color (0.10, 0.10, 0.20) /* dark blue */
color (0.10, 0.10, 0.20) /* dark blue */
color (0.25, 0.25, 0.35) /* pale blue */
color (0.10, 0.10, 0.20) /* dark blue */
);

/* Multiply this color by the diffusely reflected light. */
Ci = Ka*ambient() + Kd*diffuse(Nf);

/* Adjust for opacity. */
Oi = Os;
Ci = Ci * Oi;

/* Add in specular highlights. */
Ci += specularcolor * Ks * specular(Nf,V,roughness);
}
```

Procedural Texture Generation

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}
```

Procedural Texture Generation

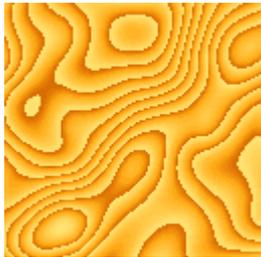
- Perlin noise
 - Solid texture
 - Based on gradient noise
 - Generate an n-dimensional lattice of random gradients
 - The noise value is interpolated in the lattice cells, e.g. using linear or cosine interpolation.
 - Gradient noise is conceptually different than value or wavelet noise.



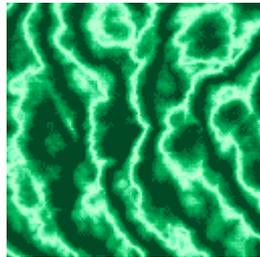
<http://www.noisemachine.com/talk1/>

Texture Functions: Perlin noise

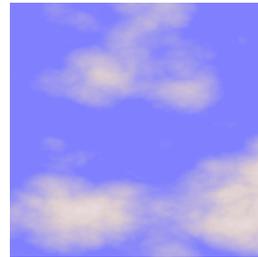
- other examples:



wood



marble



clouds

Images by Matt Zucker



see also ShaderToy „Perlin Noise“, e.g.

<https://www.shadertoy.com/view/Md3SzB>

<https://www.shadertoy.com/view/4tdSWr>

Image by Ken Perlin

Texture Functions

- wood shader



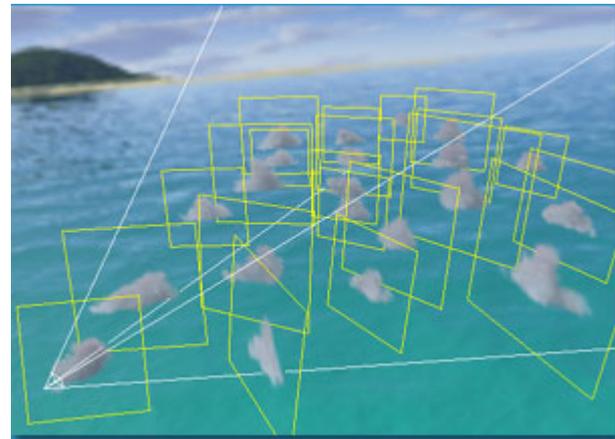
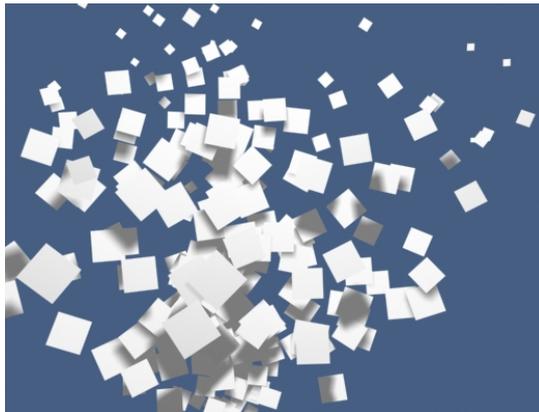
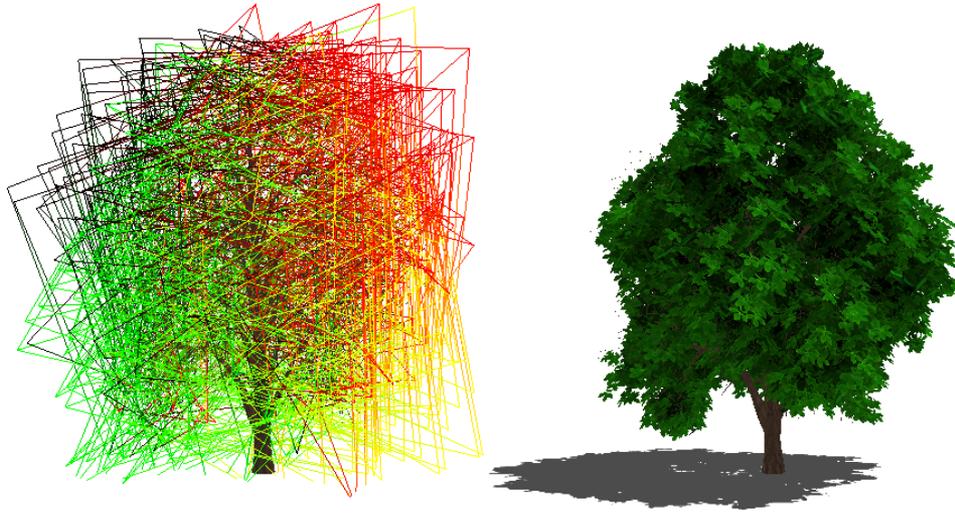
<http://flycooler.com/>



bertramguitars.com

Texture Mapping

- many other applications for textures



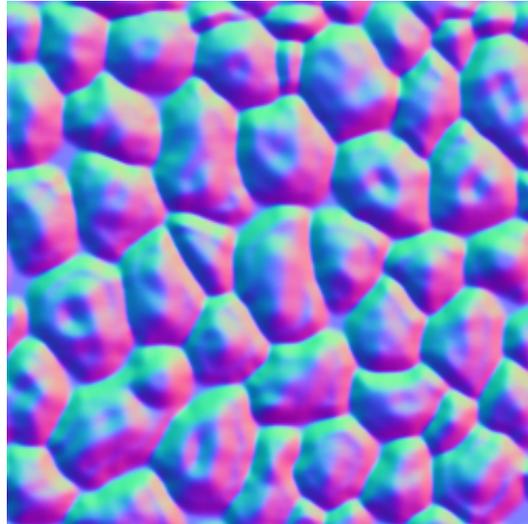
Textures Beyond Wallpaper: Normal Maps

- Non-Graphics Application: „Solarscreens“



Textures Beyond Wallpaper: Normal Maps

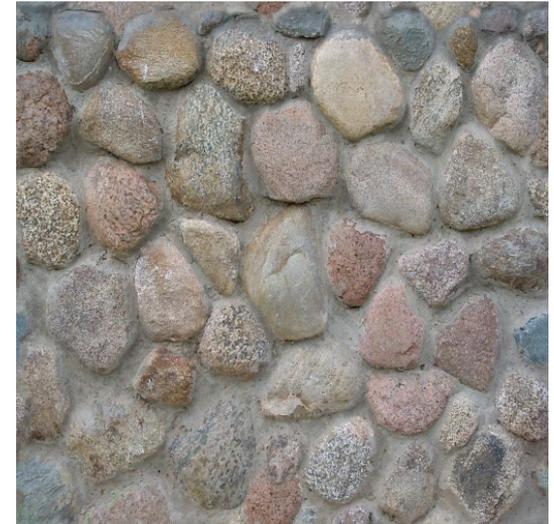
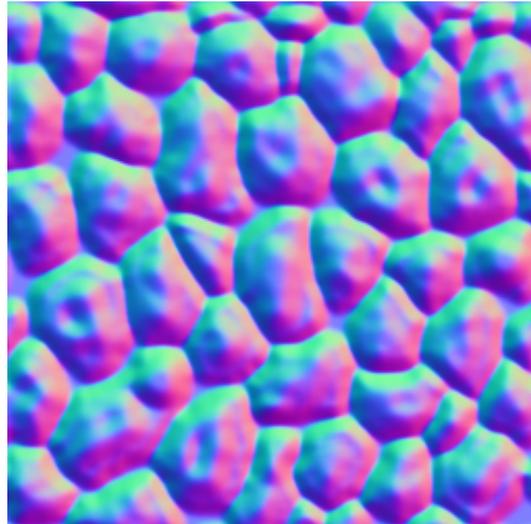
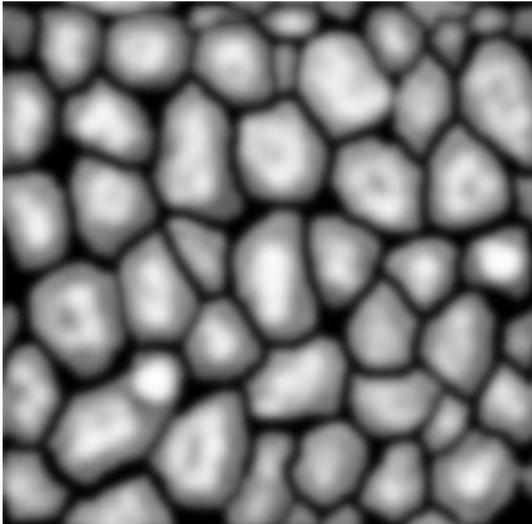
- Normal Map
 - texture with 3D normals encoded in RGB
 - 8 Bit per component sufficient
 - but also 3x10 Bit, 4x16 Bit unsigned, floating point
 - [-1,1] to [0;1]
 - $R = x/2 + 0.5$, $G = y/2 + 0.5$, ...
 - $x = 2R - 1$, ...



Textures Beyond Wallpaper: Normal Maps

- from height fields
 - local differences:

$$N(x, y) = \begin{pmatrix} 2\Delta x \\ 0 \\ h(x + \Delta x, y) - h(x - \Delta x, y) \end{pmatrix} \times \begin{pmatrix} 0 \\ 2\Delta y \\ h(x, y + \Delta y) - h(x, y - \Delta y) \end{pmatrix}$$



Normal Maps

- Multiple Textures

```
gl.activeTexture(gl.TEXTURE0);  
gl.bindTexture(gl.TEXTURE_2D,color);  
  
gl.activeTexture(gl.TEXTURE1);  
gl.bindTexture(gl.TEXTURE_2D,normalmap);
```

- Pixel Shader

```
...  
uniform sampler2D color,normalmap;  
varying vec2 uv; // texture coordinate  
  
void main(void) {  
    ...  
    vec3 c = texture2D(color,uv);  
    vec3 n = texture2D(normalmap,uv);  
    float diff = dot(n,light);  
    ...  
    gl_FragColor = ...  
}
```

Texture Mapping Demo

Textures



Texture Magnification

NEAREST

LINEAR

Texture Minification

NEAREST - No MIPMap

LINEAR - No MIPMap

NEAREST_MIPMAP_NEAREST

LINEAR_MIPMAP_NEAREST

NEAREST_MIPMAP_LINEAR

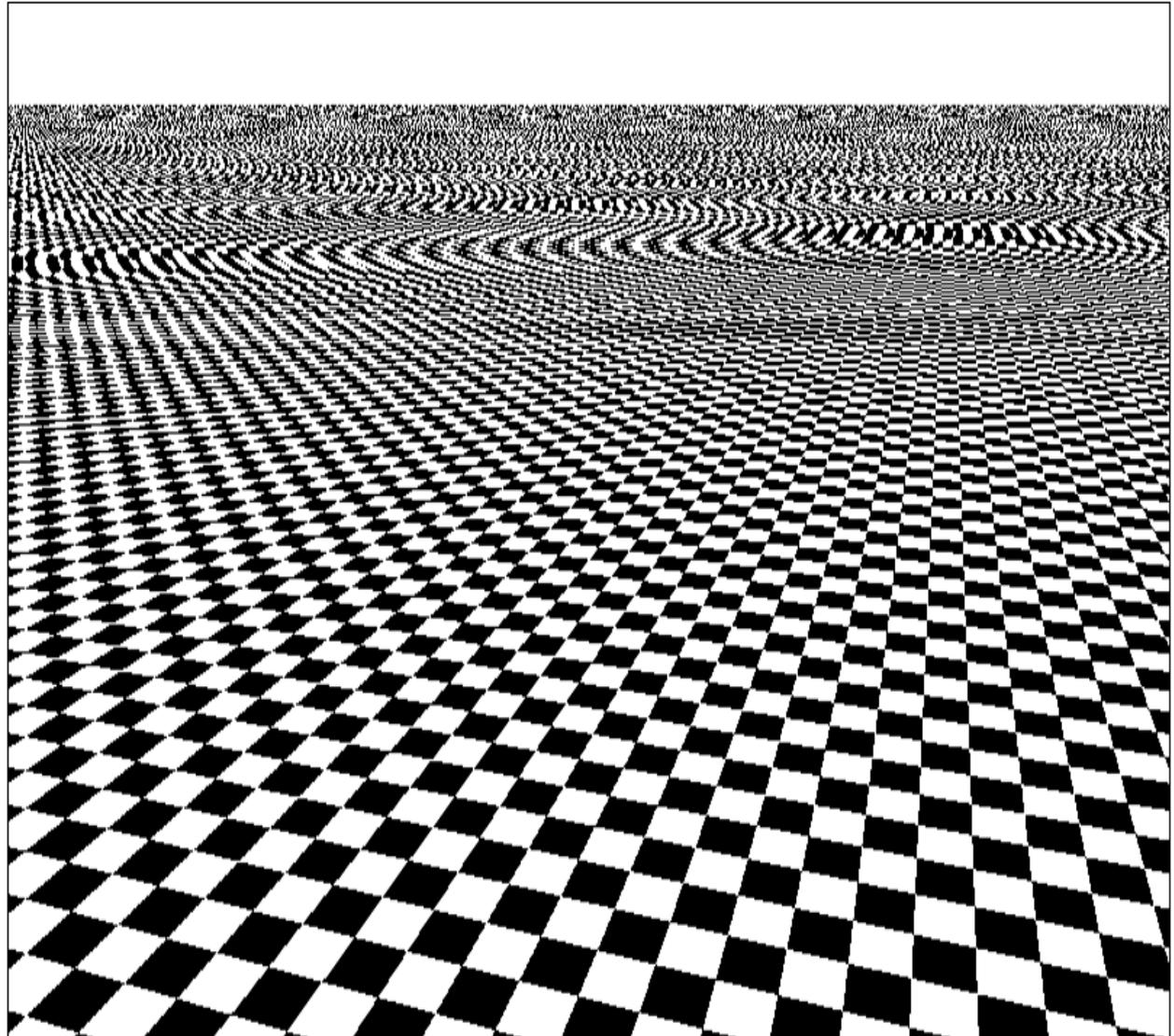
LINEAR_MIPMAP_LINEAR

Patch

Infinite Patch

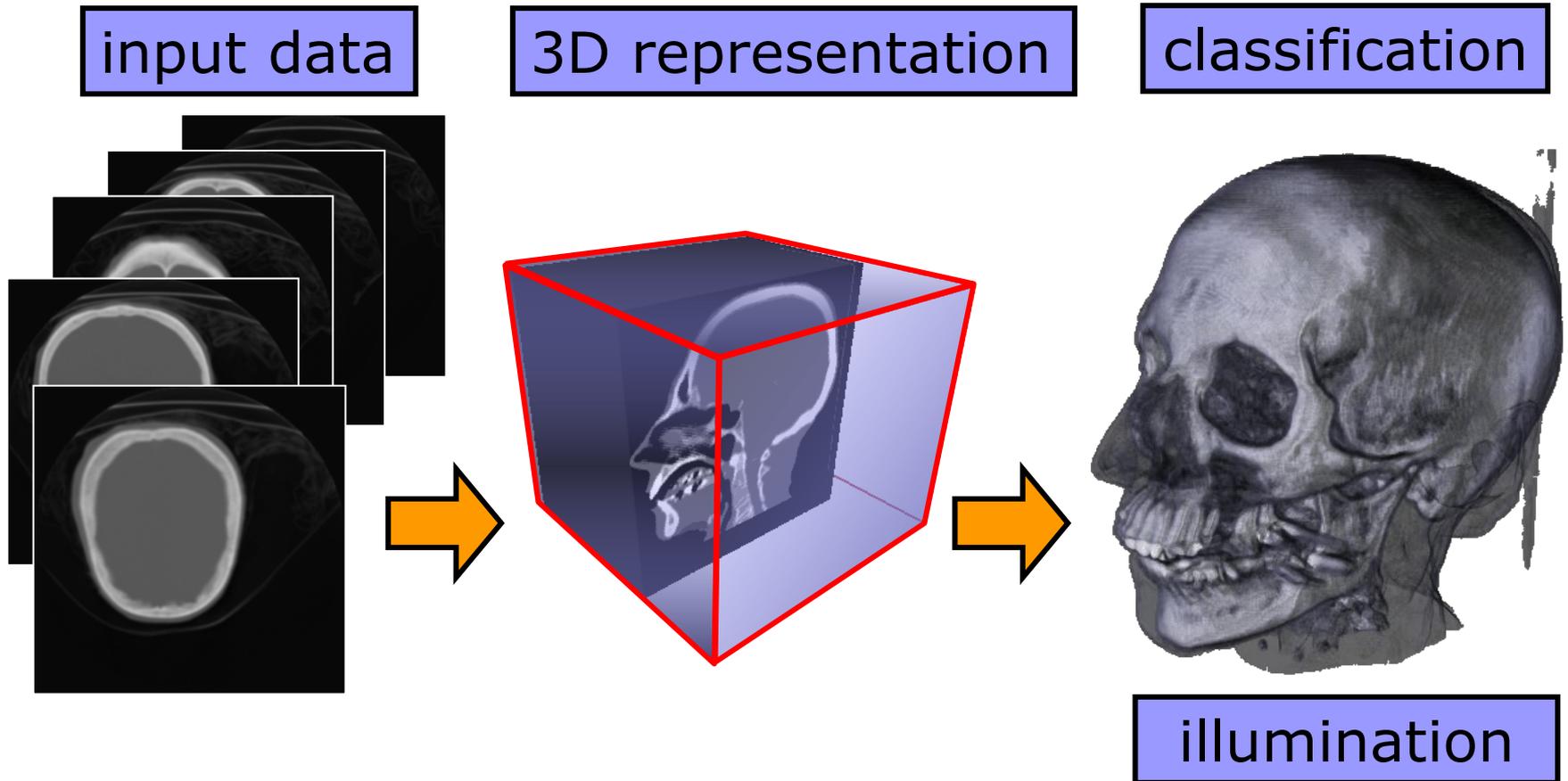
Mirror Patch

Normal Map



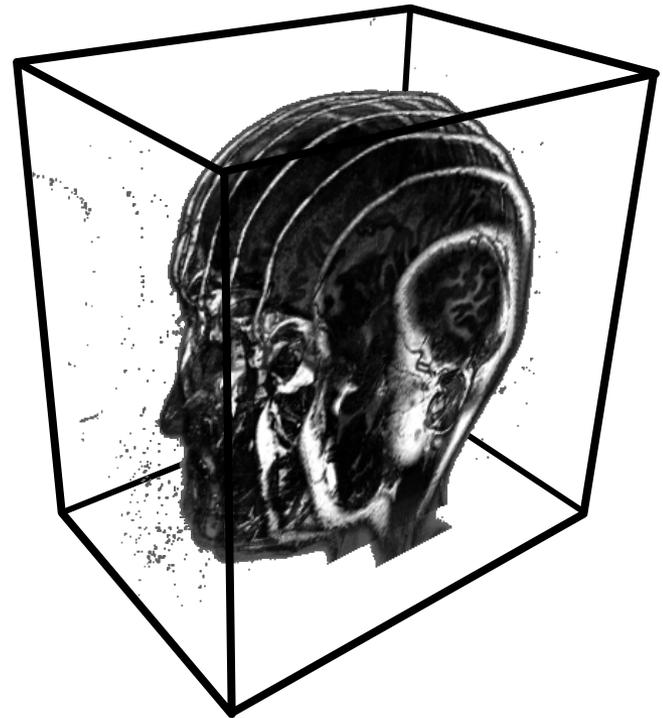
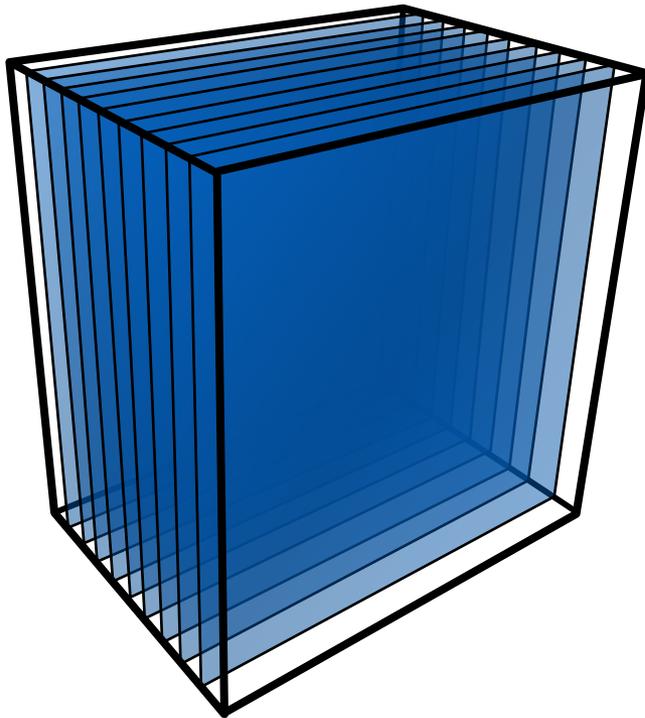
Volumetric Texture Mapping

- e.g., slices from CT data form a **volumetric texture**



Volumetric Texture Mapping

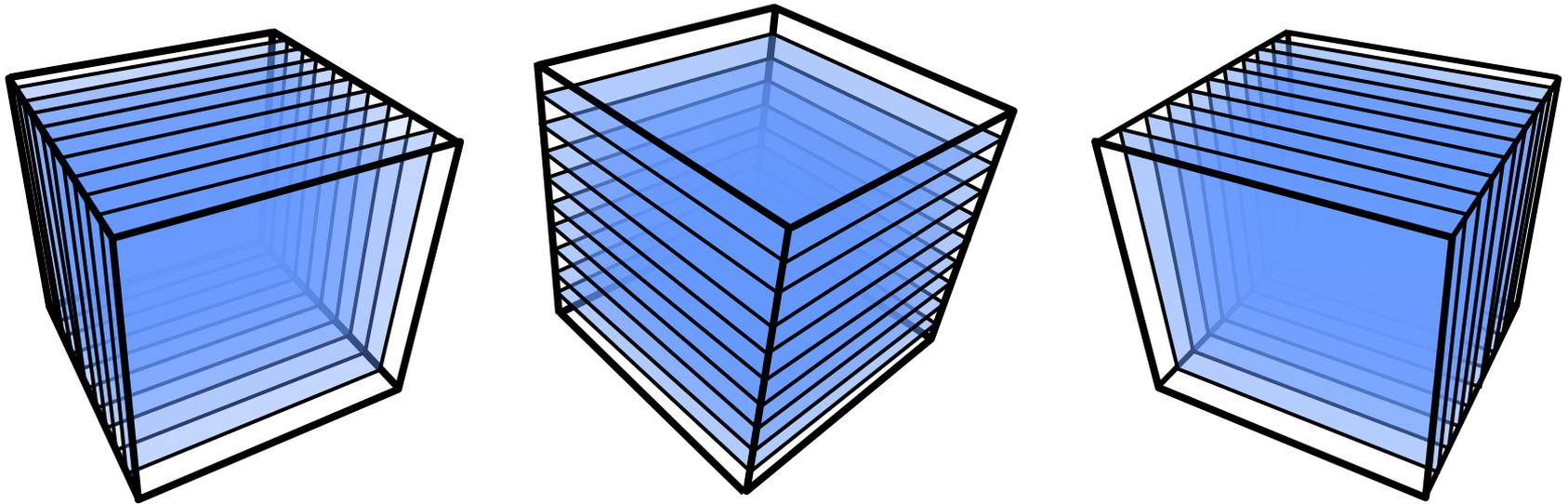
- How to render?
 - Polygonal slices with transparent textures



Christoph Rezk-Salama

Volumetric Texture Mapping

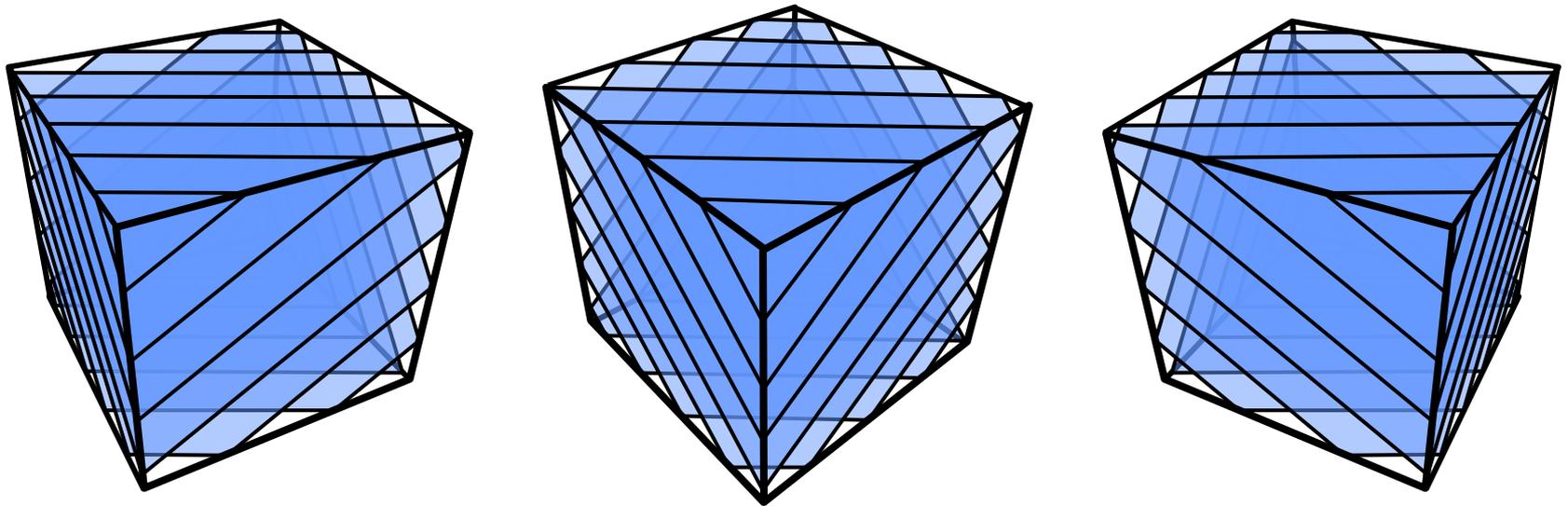
- Variant 1: Axis-aligned slices with 2D textures
→ 3 copies of the data required



Christoph Rezk-Salama

Volumetric Texture Mapping

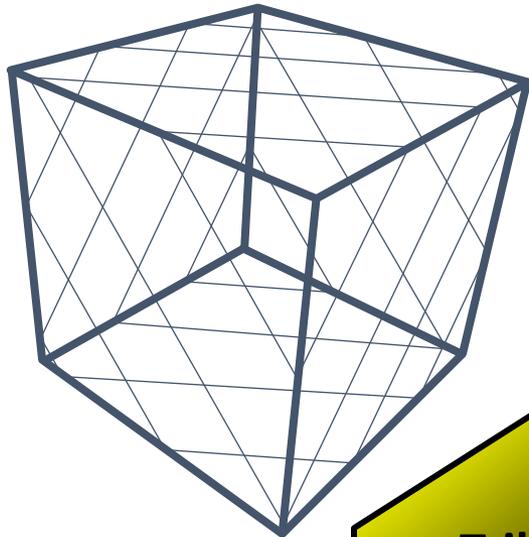
- Better: store as 3D texture (supported by OpenGL etc.)
→ 3D texture coordinates required
- Render slices parallel to image plane back to front
→ only one copy in texture memory required



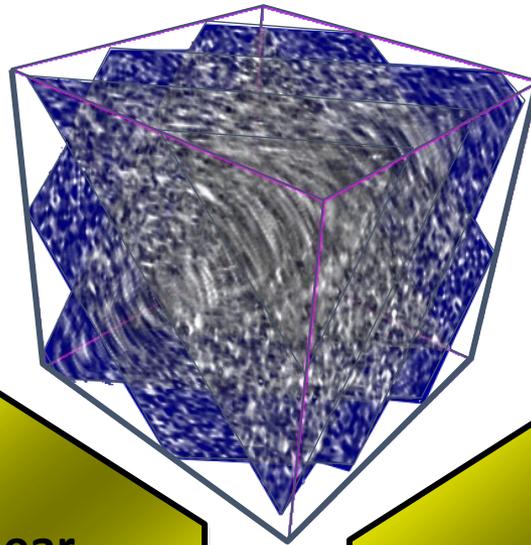
Christoph Rezk-Salama

Volumetric Texture Mapping

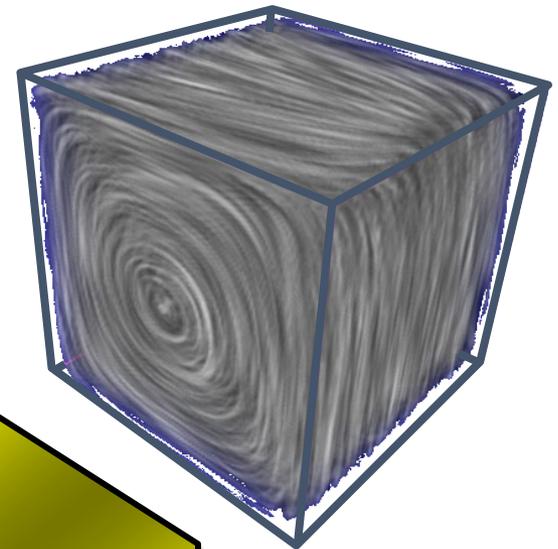
slices parallel
to image plane



texturing
polygons



final
image



**Trilinear
hardware
interpolation**

α -Blending

Christoph Rezk-Salama

Next Lecture

- How to interpolate textures
- Texture Aliasing and Antialiasing